

Relaxation and black hole feeding rates in non-spherical galactic nuclei



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Plan of the talk

- Orbits around black holes in non-spherical nuclei
- Difference between spherical, axisymmetric and triaxial nuclear star clusters
- Two-body relaxation in galactic nuclei
- Empty and full loss cone regimes
- Fokker-Planck models and N-body simulations
- Predictions for realistic galaxies; conclusions.

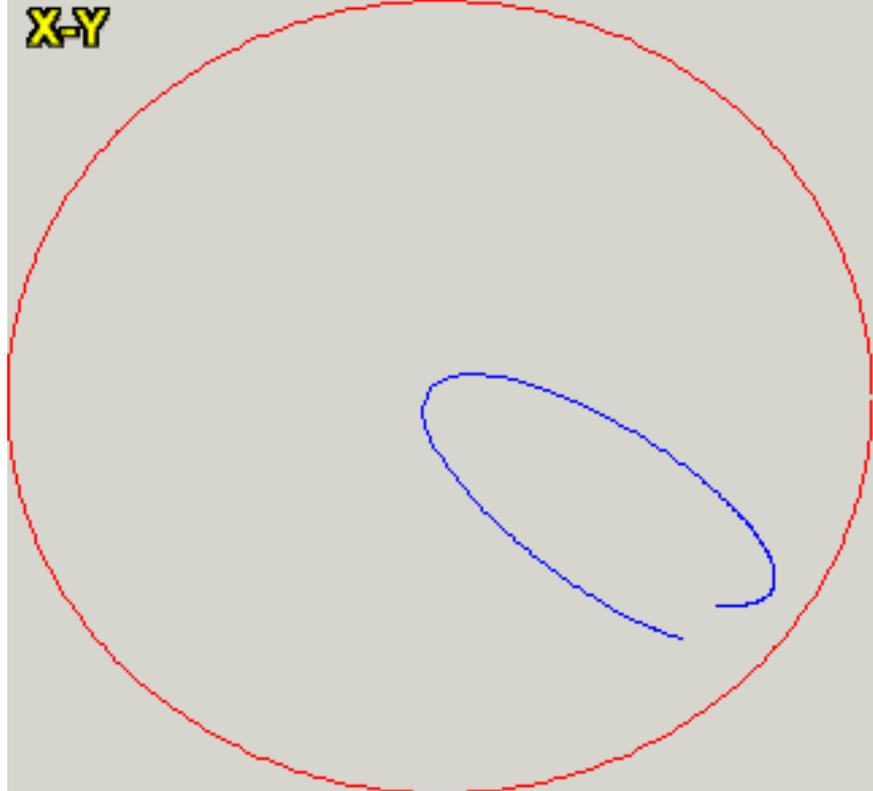
Nuclear star clusters

- Supermassive black hole M_{bh}
- Stellar cusp (for example, a power law density profile $\rho \sim r^{-\gamma}$)
- Total gravitational potential:

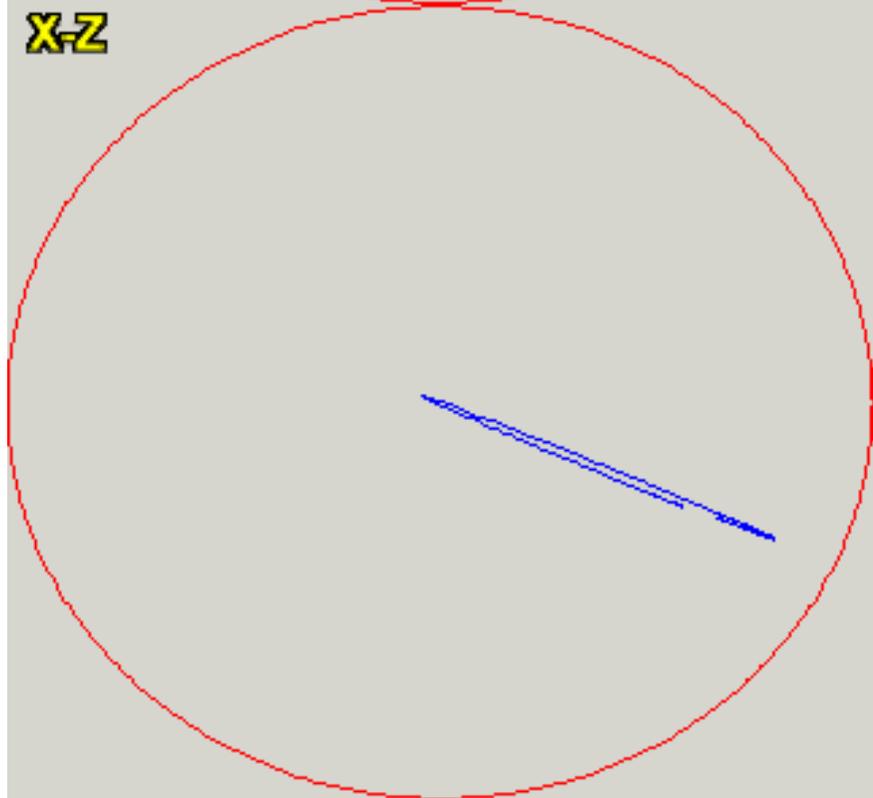
$$\Phi(\vec{r}) = -\frac{GM_{bh}}{r} + \Phi_{\star} \left(\frac{r}{r_0} \right)^{2-\gamma} \left(1 + \varepsilon \frac{z^2}{r^2} + \eta \frac{y^2}{r^2} \right)$$

- Consider motion inside radius of influence $r_{infl} \Rightarrow$
dominant contribution is from SMBH \Rightarrow
orbits are perturbed Keplerian ellipses
which precess due to torques from stellar potential
(motion outside r_{infl} is discussed towards the end of talk).
- Orbital time $t_{orb} \ll$ precession time $t_{prec} \sim r_{infl}/\sigma$

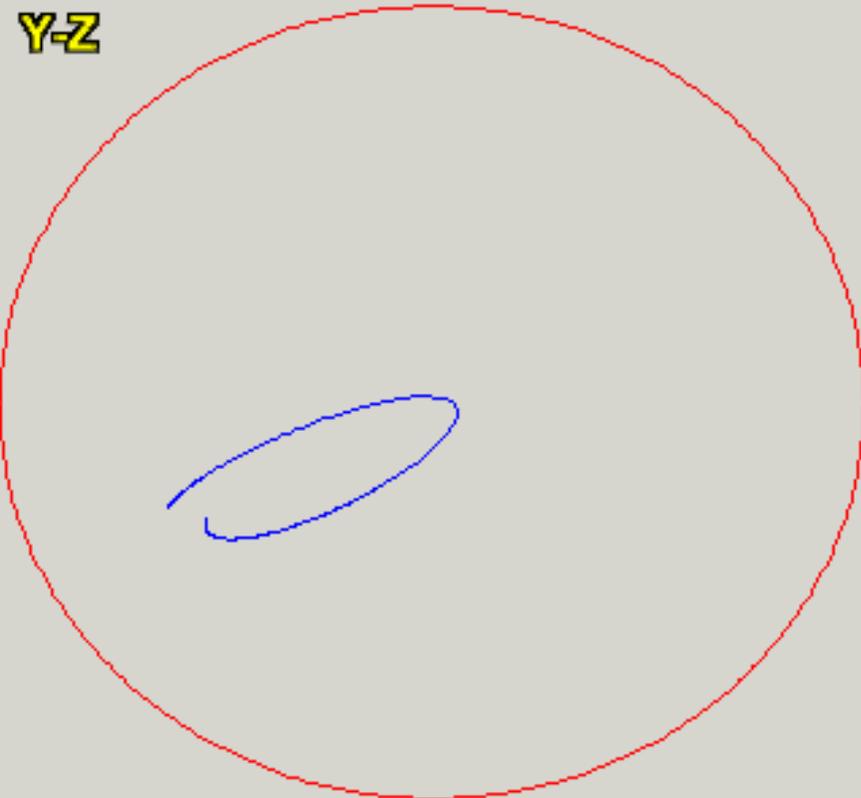
X-Y



X-Z

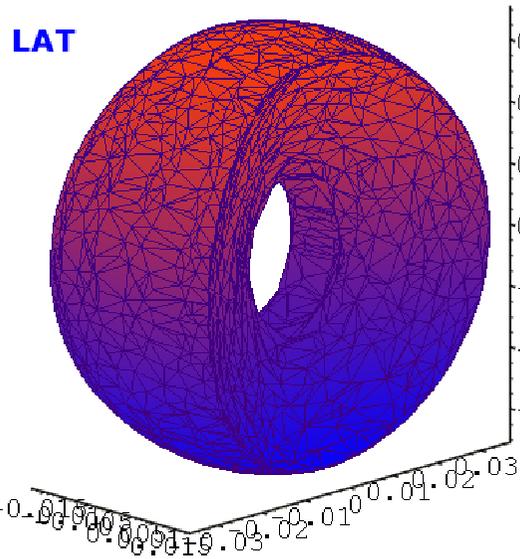


Y-Z

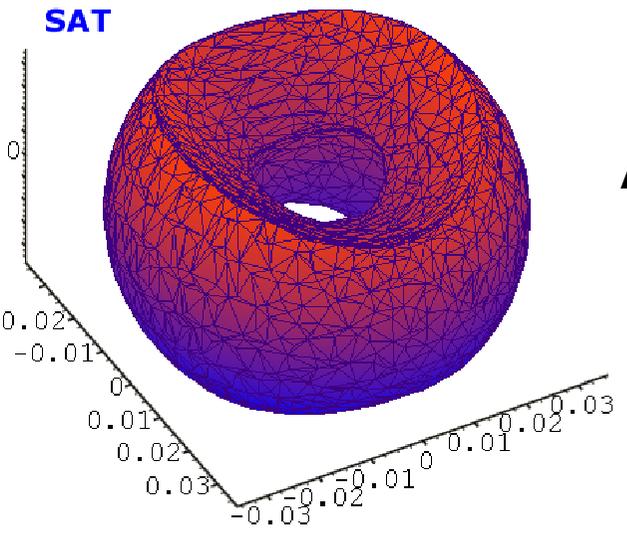


Types of orbits in non-spherical star cluster around a supermassive black hole

Triaxial cluster:

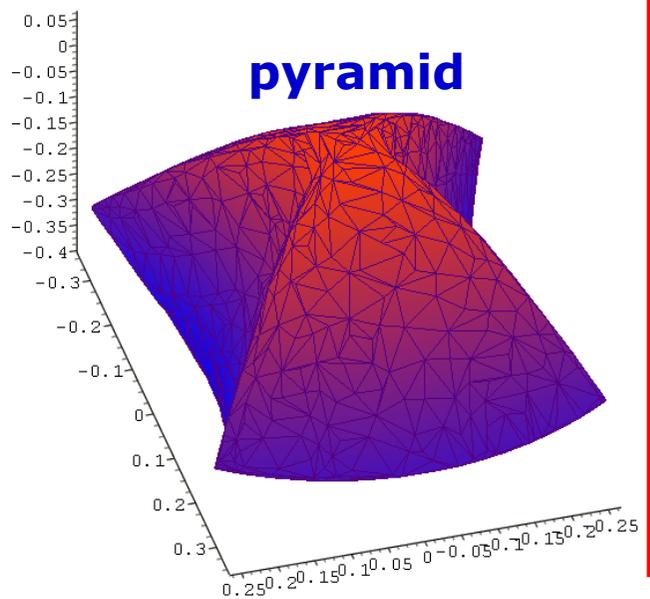


SAT

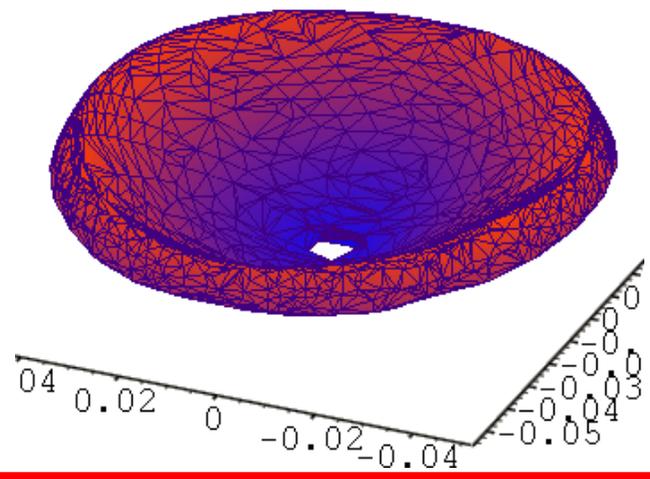


Axisymmetric cluster

pyramid

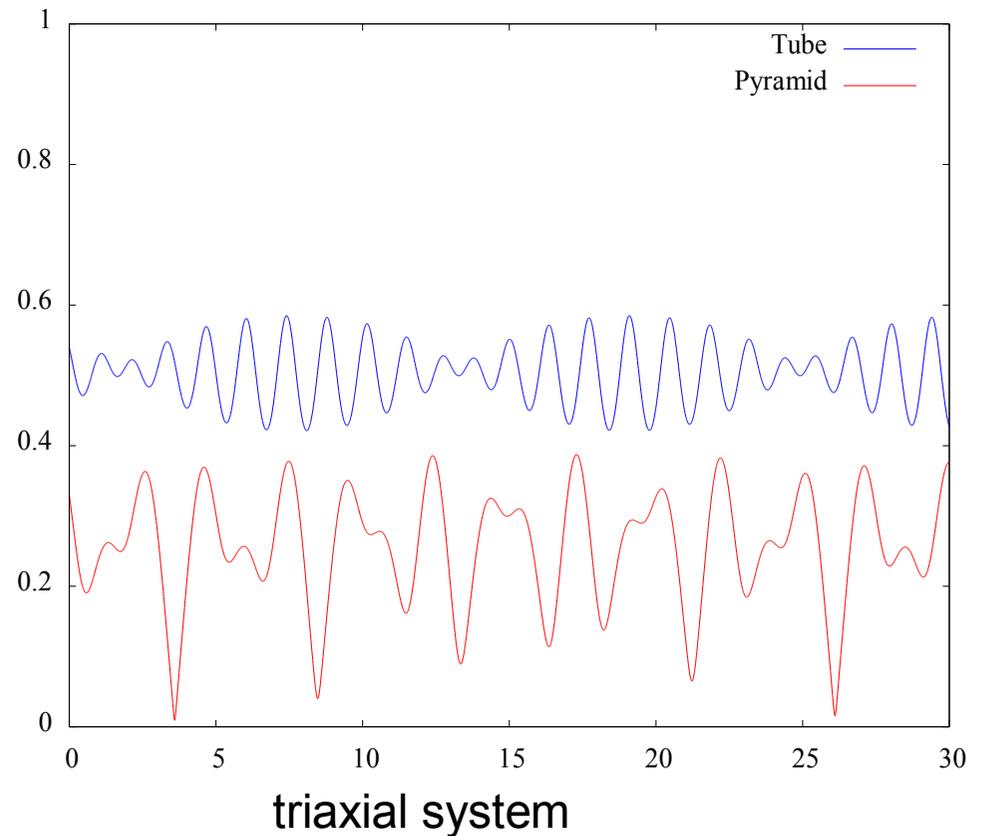
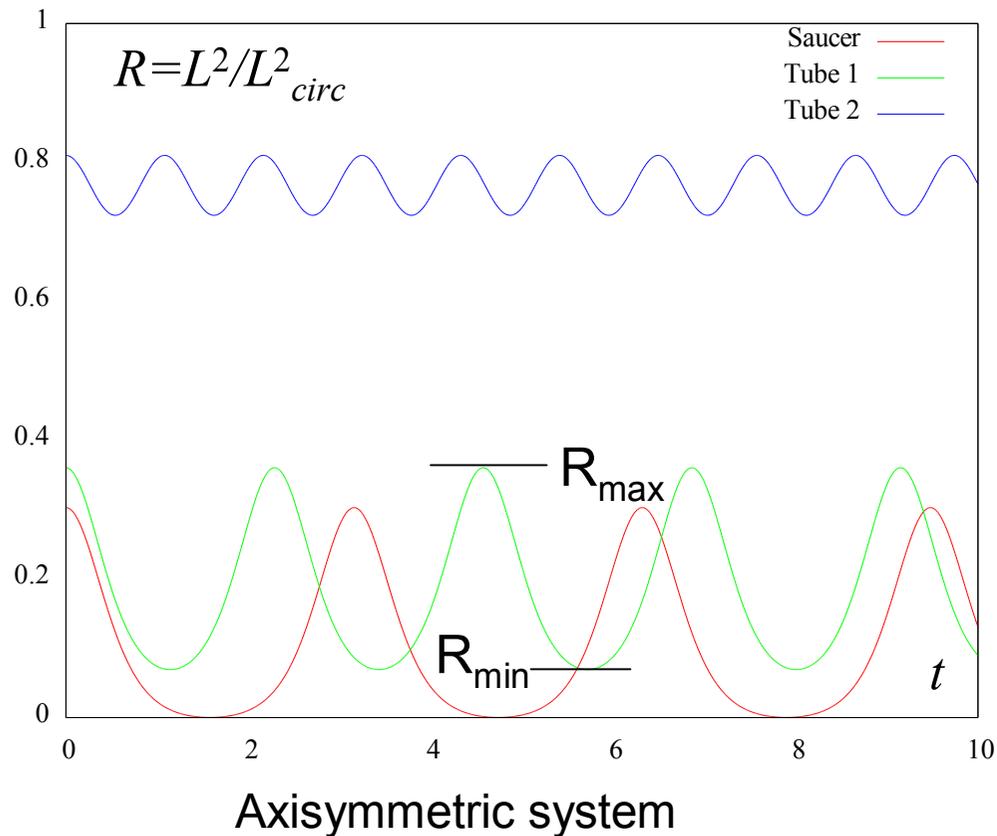


saucer



Evolution of angular momentum of an orbit in a non-spherical nuclear star cluster

Three integrals of motion: total energy E , secular hamiltonian H , and a third integral which is reduced to z-component of angular momentum L_z in axisymmetric systems. Total angular momentum squared, L^2 , is not conserved but experiences oscillations between R_{\min} and R_{\max} with characteristic period $T_{\text{osc}} \sim T_{\text{prec}}$, and amplitude $\sim \varepsilon$.



Difference between spherical, axisymmetric and triaxial nuclear star clusters

| | Spherical | Axisymmetric | Triaxial |
|--|--------------------------------------|--------------------------------------|---------------------------------|
| Fraction of stars with $L^2_{\min} < X$ | $\propto X$ | $\propto \sqrt{X\varepsilon}$ | $\propto \varepsilon$ |
| Fraction of time that such a star has $L^2 < X$ | 1 | \sqrt{X} | X |
| Survival time of such stars (assuming they are captured immediately after reaching $L^2 < R_{\text{capt}}$) | T_{rad} (10^{1-5} yr) | T_{osc} (10^{5-6} yr) | may be longer than 10^{10} yr |

(for MW nucleus)

but that may not be true
in the presence of relaxation

Two-body relaxation in galactic nuclei and the concept of empty/full loss cone

Relaxation time $T_{rel} = \frac{0.34 \sigma(r)^3}{G^2 \bar{m}_* \rho_*(r) \ln \Lambda}$ – timescale for diffusion in E and L

Loss cone is the region in phase space in which an orbit is captured on the nearest pericenter passage, i.e. at most within 1 radial period, having $L^2/L_{circ}^2 = R < R_{lc}$.

The question is how fast the changes in L occur compared to radial period:

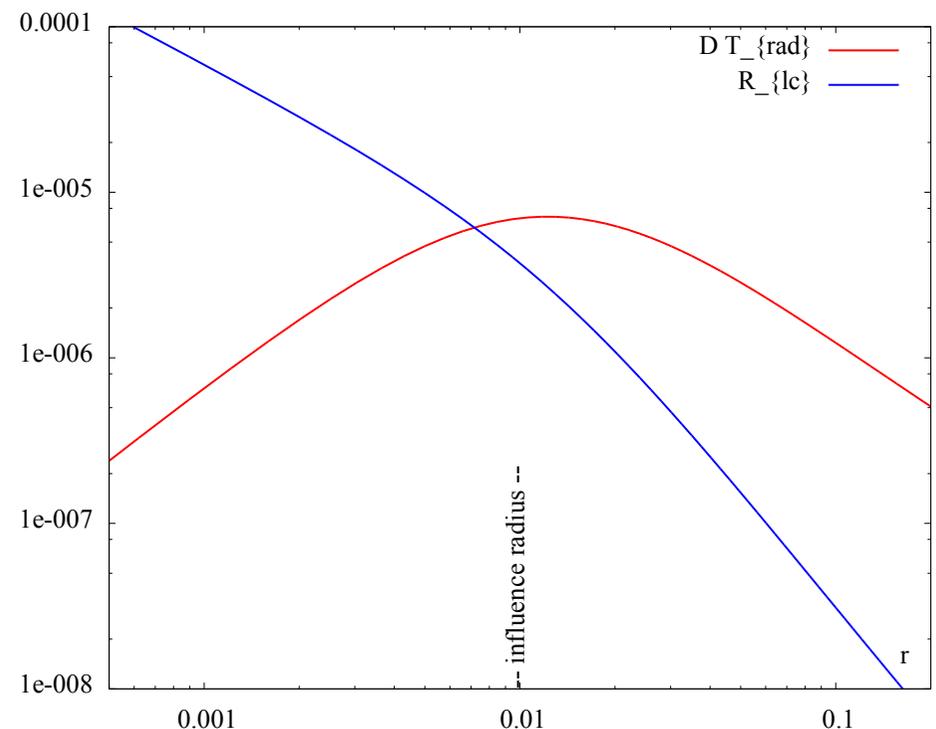
$$q = \Delta R^2 / R_{lc}^2,$$

$q \ll 1$ – empty loss cone regime:

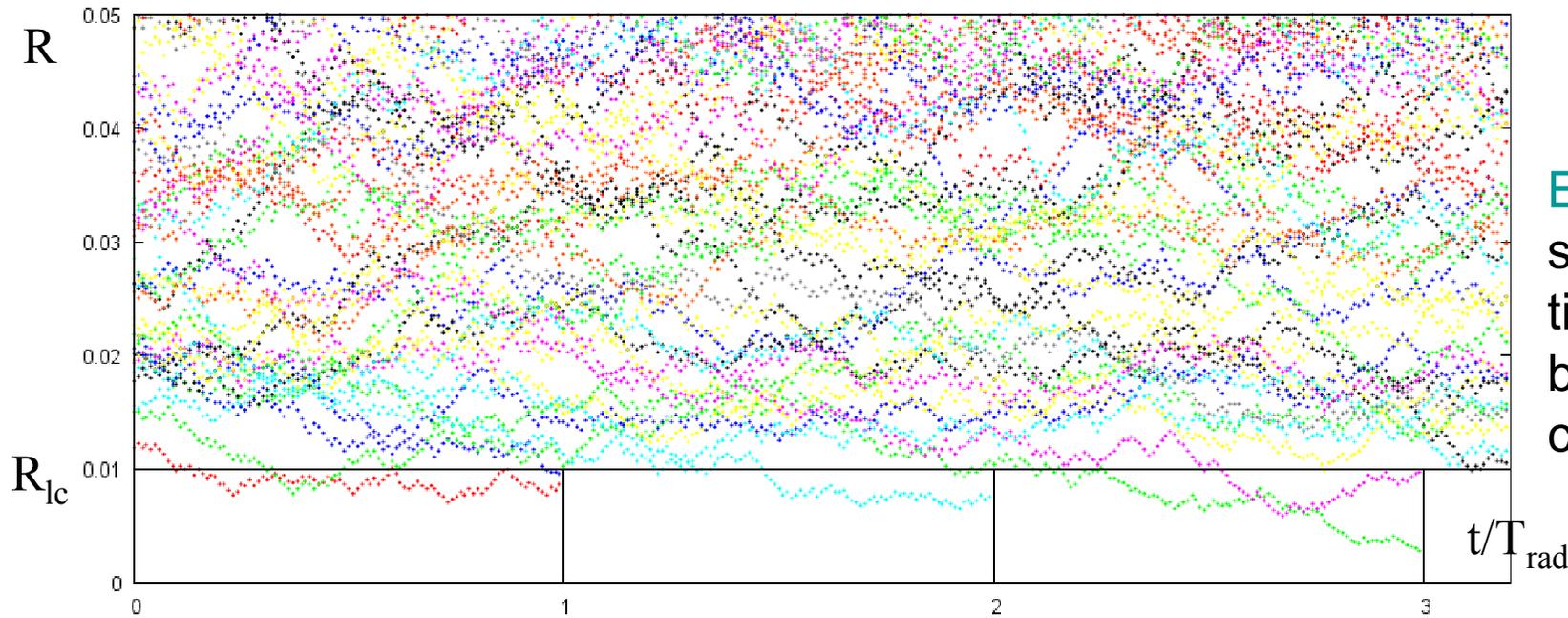
stars are captured as soon as they enter LC;
population of stars with $L^2 < R_{lc}$ is negligible

$q \gg 1$ – full loss cone:

stars may move in and out of LC many times
before being captured at the end of T_{rad} ,
d.f. of stars in LC is the same as elsewhere

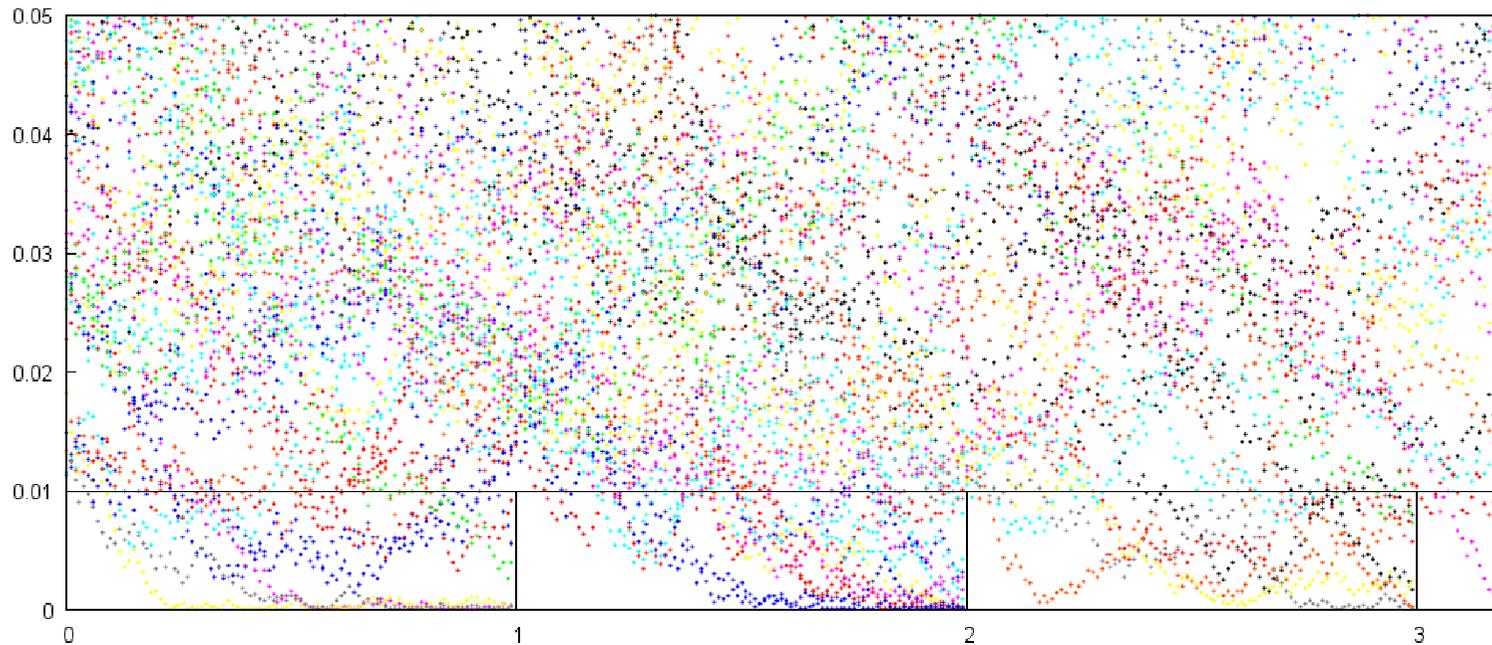


The concept of empty/full loss cone

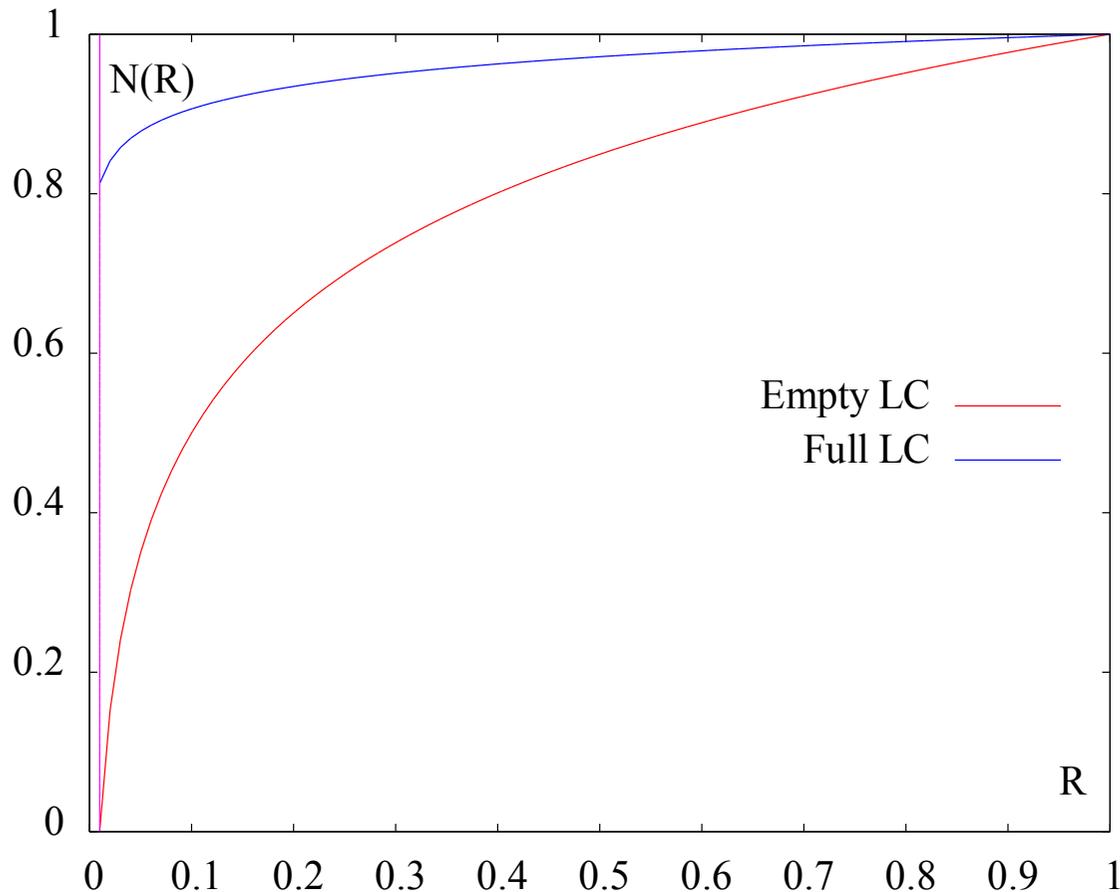


Empty LC:
stars barely have time to enter LC before they get captured after T_{rad}

Full LC:
stars may enter and exit LC many times during one T_{rad}



The concept of empty/full loss cone



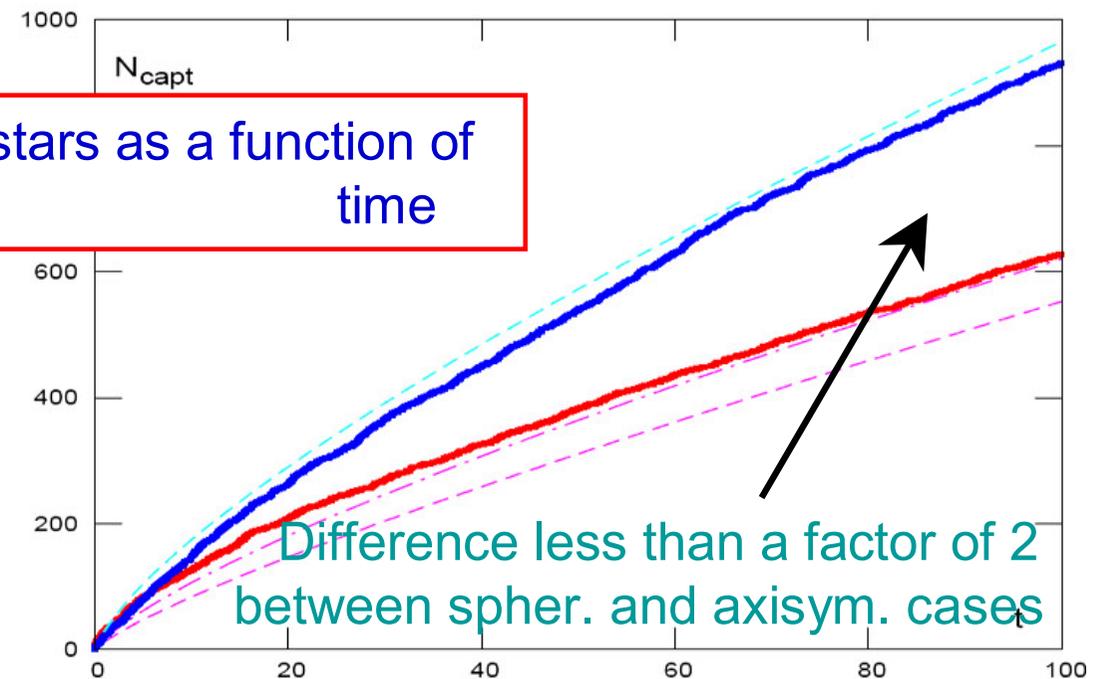
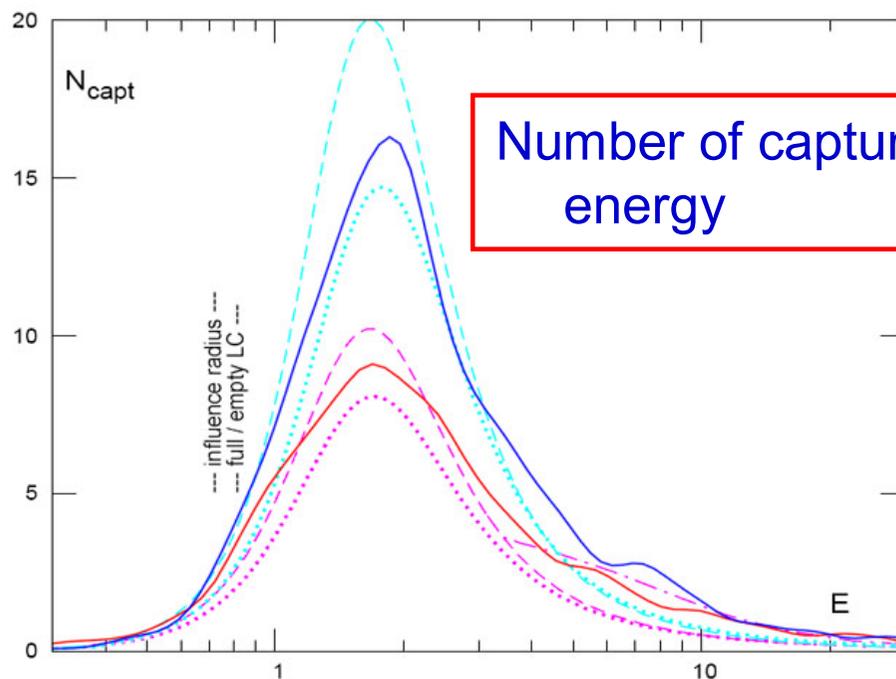
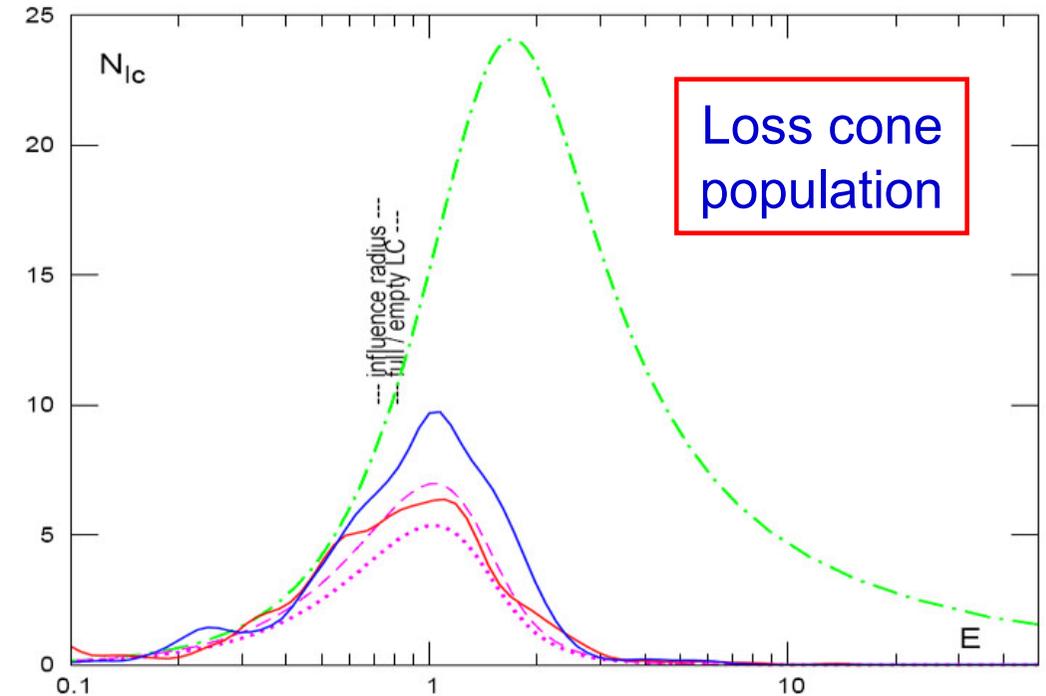
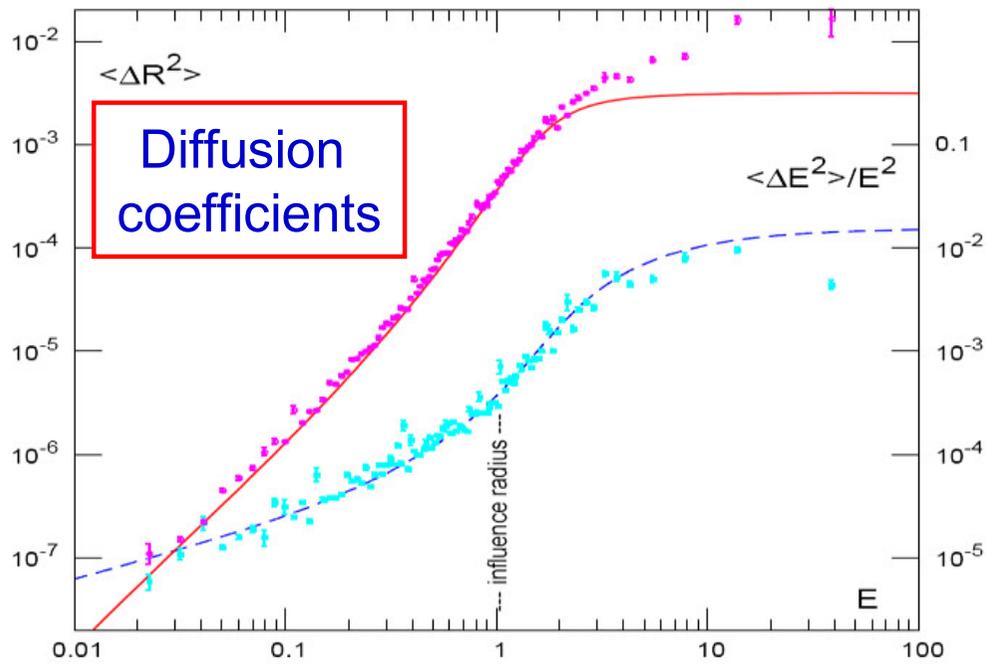
- In the empty LC regime, $N(R_{lc}) \sim 0$, $N(R) \sim \log R$, capture rate is limited by diffusion (gradient of $N(R)$): $F \sim T_{rel}^{-1} / (\log(1/R_{lc}) - 1)$ for standard 2-body relaxation
- In the full LC regime, $N(R_{lc}) \sim N(R) \sim 1$, capture rate is $F \sim R_{lc} / T_{rad}$

does not depend on diffusion coefficient or even on the mechanism of LC refill as long as it is efficient enough to keep it full!

Loss cone draining vs. relaxation

- Regular precession may shuffle stars in angular momentum more efficiently than 2-body relaxation
- The capture rate cannot exceed $F_{\text{full LC}}$, but can be larger than in the spherical case if it was in the empty loss cone regime
- After all orbits with $L_{\text{min}}^2 < R_{\text{capt}}$ have been drained, the influx of stars from higher L is still limited by diffusion (relaxation in angular momentum)
- For triaxial nuclei, the draining time of pyramid orbits may be $>10^{10}$ yr. For axisymmetric systems, adequate description of relaxation is needed (in terms of Fokker-Planck equation in terms of the variables which are integrals of motion in the absence of relaxation).
- Comparison with N-body simulations to determine applicability of F-P description; extrapolation of F-P results into the range of parameters inaccessible for direct N-body.

Comparison of Fokker-Planck models with N-body simulations



Number of captured stars as a function of energy

Conclusions

- In non-spherical nuclear star clusters the star angular momentum L is changed not only due to 2-body relaxation, but also due to regular precession
- This facilitates the capture of stars at low L :
the “expanded” loss region is where $L_{\min}^2 < L_{\text{capt}}^2$, not just $L^2 < L_{\text{capt}}^2$
- Draining time of this region is $\sim T_{\text{prec}} \sim 10^{5-6}$ yr in axisymmetric case and much longer, comparable to Hubble time, in triaxial case
- Compared to the spherical case, the difference in total capture rate for axisymmetric case is relatively small (\sim factor of 2) and is important only in the transition regime between empty and full loss cone
- For giant elliptical galaxies, which are deeply in the empty loss cone regime for a spherical case, the enhancement may be more dramatic